

Describe objects by proximity, position, and direction, using terms such as near, far, below, above, up, down, behind, in front, next to, left, and right.	*	X	X	X	X	X	X	X	X
Sort objects and data by commonalities and classify them into categories; reclassify the objects or numbers in a set according to a different set of criteria or characteristics.	*	X	X	X	X	X	X	X	X
Collect data about the students and their surroundings on charts, using tally marks to record the data.	*	X	X	X	X	X	X	X	X
Compare data (e.g. largest, smallest, most, least often) and represent the data using picture graphs or bar graphs.	*	X	X	X	X	X	X	X	X
Draw conclusions by interpreting data from a simple picture or bar graph.	*	X	X	X	X	X	X	X	X
Compare whole numbers ranging from 1 to 100 using the symbols for less than, equal to, or greater than.		*	X	X	X	X	X	X	X
Identify 1 more, 1 less, 10 more, 10 less than a given number.		*	X	X	X	X	X	X	X
Recognize and memorize the addition facts with sums up to 20, as well as the corresponding subtraction facts; use pictures, models, and groupings to demonstrate these facts.		*	X	X	X	X	X	X	X
Recognize the logical connection between addition and subtraction (an inverse relationship), and make decisions about how to use this relationship in problem-solving situations.		*	X	X	X	X	X	X	X
Recognize equivalent forms of the same number through the use of physical models and manipulatives, diagrams and drawings, or number sentences (e.g., $3 + 3 = 4 + 2$).		*	X	X	X	X	X	X	X
Solve addition and subtraction number sentences with one- and two-digit numbers; use this process in solving mathematical and real-world problems.		*	X	X	X	X	X	X	X
Find the sum of three one-digit numbers.		*	X	X	X	X	X	X	X
Make estimates when comparing larger and smaller numbers in addition or subtraction; then, check to verify whether or not the estimates were reasonable.		*	X	X	X	X	X	X	X
Count backward from 30.		*	X	X	X	X	X	X	X
Identify odd and even numbers from 1 to 12.		*	X	X	X	X	X	X	X
Identify an element that does not belong in a simple pattern.		*	X	X	X	X	X	X	X
Tell time to the nearest half hour (before and after) and relate time by comparisons (shorter, longer, using analog and digital clocks).		*	X	X	X	X	X	X	X
Combine, pennies, nickels and dimes to equal one dollar.		*	X	X	X	X	X	X	X
Distinguish between two-dimensional and three-dimensional shapes.		*	X	X	X	X	X	X	X
Explore the symmetries of objects and shapes.		*	X	X	X	X	X	X	X

Begin to develop a spatial sense by giving and following directions about the location of objects.		*	X	X	X	X	X	X	X
Use words, models, pictures, and groups of objects to represent numbers.			*	X	X	X	X	X	X
Identify numbers as combinations of tens and ones.			*	X	X	X	X	X	X
Recognize the purpose of zero as a placeholder, and describe what happens when zero is added or subtracted from a number.			*	X	X	X	X	X	X
Use the symbols $<$, $=$, $>$ to compare and order whole numbers to 1,000; use other qualitative terms (bigger, taller, slower, same as) to make comparisons (using formal, as well as mathematical language)			*	X	X	X	X	X	X
Read number words and ordinal numbers through 100.			*	X	X	X	X	X	X
Round one and two digit numbers to the nearest 10.			*	X	X	X	X	X	X
Demonstrate fluency in knowing addition and subtraction facts through 20; add and subtract multiples of 10.			*	X	X	X	X	X	X
Use mental math to find the sum or difference of two two-digit numbers that do not require regrouping.			*	X	X	X	X	X	X
Solve addition problems (with and without regrouping) and subtraction problems (without regrouping) using up to three digit numbers.			*	X	X	X	X	X	X
Demonstrate understanding of the relationship of odd and even numbers in addition and subtraction (e.g. two odd numbers equals an even number)			*	X	X	X	X	X	X
Begin to study division through the use of repeated subtraction and forming equal groups from a single set.			*	X	X	X	X	X	X
Recognize that fractions such as $\frac{3}{3}$ and $\frac{7}{7}$, where all fractional parts are included, are equal to one or one whole.			*	X	X	X	X	X	X
Represent numbers in equivalent ways.			*	X	X	X	X	X	X
Begin to use symbols within a number sentence to indicate unknown quantities.			*	X	X	X	X	X	X
Relate problem situations to corresponding addition or subtraction number sentences; make decisions about and explain the strategies to be used.			*	X	X	X	X	X	X
Evaluate the reasonableness of a solution by considering appropriate estimates and by considering the context of the original problem.			*	X	X	X	X	X	X
Improve in problem-solving by prioritizing pertinent information and disregarding irrelevant information.			*	X	X	X	X	X	X
Recognize that adding numbers in any order results in the same sum; recognize that adding numbers grouped in any order results in the same sum; explore why these rules do not apply to subtraction.			*	X	X	X	X	X	X

Identify and extend linear numerical patterns; use patterns to solve problems.			*	X	X	X	X	X	X
Identify a nonstandard unit of measure and iterate that unit to measure the length of an object. Then use a standard unit of measure and compare the results.			*	X	X	X	X	X	X
Measure an object to the nearest inch, foot, yard, centimeter, and meter.			*	X	X	X	X	X	X
Use different standard units of measurement when making estimates, recognize if the estimate is reasonable, and use the appropriate tool to check on the validity of the estimate.			*	X	X	X	X	X	X
Demonstrate the relationship of various measure of time.			*	X	X	X	X	X	X
Tell time to the nearest quarter and half hour, using analog and digital clocks, distinguish between a.m. and p.m.			*	X	X	X	X	X	X
Recognize and use the dollar and cent symbols and the proper placement of the decimal point to indicate amounts of money.			*	X	X	X	X	X	X
Use addition and subtraction to solve problems involving combinations of coins and bills.			*	X	X	X	X	X	X
Describe and classify common geometric two- and three-dimensional objects using characteristics such as number and shape of faces, edges, and angles, and identifying these shapes within the classroom environment.			*	X	X	X	X	X	X
Identify two-dimensional shapes that are congruent or similar.			*	X	X	X	X	X	X
Create symmetrical patterns, shapes, and designs.			*	X	X	X	X	X	X
Collect and record data in systematic, categorical way; interpret the data on a graph or chart by asking and answering simple questions.			*	X	X	X	X	X	X
Use the data on a graph or chart to demonstrate a conclusion in the form of an addition or subtraction number sentence; explain the reasoning used in making the conclusion.			*	X	X	X	X	X	X
Make comparative verbal and numerical descriptions of the range of data on a chart or graph.			*	X	X	X	X	X	X
Determine the mode in a series of charted or graphed items; represent data in more than one way			*	X	X	X	X	X	X
Recognize patterns in graphed data; identify inappropriate or false conclusions about a set of data; and, on the basis of the data, predict if something is more or less likely to occur.			*	X	X	X	X	X	X
Compare, order, read, and write numbers to 10,000.			*	X	X	X	X	X	X
Identify the place value for each digit in numbers to 10,000; use expanded notation to represent this.			*	X	X	X	X	X	X
Round off numbers to the nearest tens, hundreds, and thousands.			*	X	X	X	X	X	X
Use addition and subtraction with numbers up to 10,000.			*	X	X	X	X	X	X
Memorize multiplication tables for numbers 1-10.			*	X	X	X	X	X	X

Explore the unique properties of 0 and 1 in multiplication and division.				*	X	X	X	X	X
Solve simple problems involving multi-digit numbers multiplied or divided by a one-digit number.				*	X	X	X	X	X
Verbalize how the remainder in a division expression could impact a real-life situation.				*	X	X	X	X	X
Represent fractions and mixed numbers with numerals, concrete materials, drawings, and words.				*	X	X	X	X	X
Locate whole and fractional numbers on a number line.				*	X	X	X	X	X
Use drawings and concrete materials to compare fractions, determining equivalency or if greater or less than.				*	X	X	X	X	X
Demonstrate that fractions and decimals are different ways to represent the same concept.				*	X	X	X	X	X
Add and subtract numbers using simple fractions or decimals.				*	X	X	X	X	X
Choose appropriate operational symbols to make an expression true.				*	X	X	X	X	X
Solve problems and demonstrate relationships of numerical quantities using expressions, equations, or inequalities, working with and without a calculator.				*	X	X	X	X	X
Apply strategies and results from simpler problems to solve more complex problems.				*	X	X	X	X	X
Recognize that the commutative and associative properties, as used with addition, also can be used with multiplication; explore why these properties do not work with subtraction and division.				*	X	X	X	X	X
Recognize and extend a linear pattern after determining its pattern or rule; recognize that unlike addition, multiplication may involve different units.				*	X	X	X	X	X
Develop and use strategies for making reasonable estimates.				*	X	X	X	X	X
Determine and use the appropriate tools and units to measure length, liquid volume and weight.				*	X	X	X	X	X
Read thermometers and compare temperatures in both Fahrenheit and Celsius				*	X	X	X	X	X
Carry out simple unit conversion within a measurement system.				*	X	X	X	X	X
Count money and make change using coins and bills up to \$10.				*	X	X	X	X	X
Identify and draw points, lines, and segments.				*	X	X	X	X	X
Make a physical model to show different angles; identify angles are right, acute, obtuse, and straight angles.				*	X	X	X	X	X
Classify and describe polygons using exact vocabulary.				*	X	X	X	X	X
Determine the perimeter of simple geometric shapes.				*	X	X	X	X	X
Explore the area and volume of solid figures through several means, such as by covering them with equal-size squares or counting the number of cubes needed to fill them.				*	X	X	X	X	X

Identify and classify common three-dimensional geometric objects and find examples in the classroom environment; recognize the shapes from a different perspective.				*	X	X	X	X	X
Explore symmetry using a mirror; find the line of symmetry of non-geometrical shapes, such as in some of the letters in the alphabet.				*	X	X	X	X	X
Find and name locations on a labeled grid or coordinate system.				*	X	X	X	X	X
Construct and interpret graphs with intervals larger than one.				*	X	X	X	X	X
Use fractions to interpret information on a timeline.				*	X	X	X	X	X
Identify the range and mode of graphed data.				*	X	X	X	X	X
Use probability experiments to predict future events as likely, unlikely, or impossible.				*	X	X	X	X	X
Design a survey or investigation to collect information regarding a given question; choose suitable procedures; display information gathered; and explain and justify the process used to draw conclusions.				*	X	X	X	X	X
Read and write numbers in the millions and use extended notation to explain the place value.					*	X	X	X	X
Determine when to round off numbers and explain the reasoning behind the decision; round off numbers to the nearest ten, hundred, thousand, ten thousand, and hundred thousand.					*	X	X	X	X
Explore the concept of negative numbers on a number line, in counting, in temperature, and in finances.					*	X	X	X	X
Apply an understanding and ability to use algorithms for adding and subtracting multi-digit numbers to solve problems.					*	X	X	X	X
Apply an understanding and ability to use algorithms for multiplying multi-digit numbers by two-digit numbers to solve problems.					*	X	X	X	X
Apply an understanding and ability to use algorithms for dividing multi-digit numbers by a one digit number to solve problems.					*	X	X	X	X
Know multiplication facts through 12 times 12 and develop use of strategies and patterns to help retention of these facts; use various models, including sets and arrays to represent multiplication facts; estimate products and quotients beyond the basic facts.					*	X	X	X	X
Use left-to-right multiplication and the distributive property to find an exact answer using mental math, without using paper, pencil or calculator.					*	X	X	X	X
Explore the numbers 2,3,5,7, and 11 as prime numbers that do not have any factors except 1 and themselves.					*	X	X	X	X
Be able to explain fractions verbally and through models or drawings as parts of a whole, parts of a set, a division of whole numbers by whole numbers, and demonstrating fractional equivalency.					*	X	X	X	X

Order and compare numbers that include decimals to two decimal places using the symbols $<$, $=$, $>$; write and compare fractions of tenths and hundredths to their decimal equivalents.					*	X	X	X	X
Rename and rewrite whole numbers as fractions; analyze improper fractions and mixed numbers; represent fractions and decimals on a number line.					*	X	X	X	X
Use letters, boxes, or other symbols to stand for any number in simple expressions, equalities, or inequalities.					*	X	X	X	X
Recognize that an equation such as $y=x+3$ can be used for finding a second number when a first number is given; demonstrate understanding of the concepts of a variable.					*	X	X	X	X
Understand and use parentheses to show which operation to perform first in an equation.					*	X	X	X	X
Manipulate equations based on an understanding that equals added to equals are equal, and equals multiplied by equals are equal.					*	X	X	X	X
Determine when to break a problem into simpler parts; apply strategies from a simpler problem to a more complex problem.					*	X	X	X	X
Analyze and solve problem situations by determining relationships, excluding irrelevant and identifying missing information, prioritizing and sequencing pertinent information, and observing patterns.					*	X	X	X	X
Express clearly, logically, verbally, and symbolically the procedures and operations used to solve a problem or draw a conclusion; recognize when a strategy does not work, and then try a new approach.					*	X	X	X	X
Use estimation, the context of a problem, and technological tools to check the reasonableness and the validity of results obtained. Determine if it is better to overestimate or underestimate in a given situation.					*	X	X	X	X
Use formulas to solve problems involving perimeters or rectangular shapes; know how perimeters relate to areas and volume.					*	X	X	X	X
Measure the area of rectangular shapes using the appropriate units.					*	X	X	X	X
Recognize volume and capacity as ways of describing the space inside a shape.					*	X	X	X	X
Use logical reasoning to make sense of monetary transactions, solving problems involving counting money and making change.					*	X	X	X	X
Make simple unit conversion within a measurement system.					*	X	X	X	X
Use formal geometric terms to identify parallel, intersecting, and perpendicular lines.					*	X	X	X	X

Identify the attributes of different triangles based on side lengths or on angle measures; use the appropriate tools and technology to draw examples of make models of them.					*	X	X	X	X
Identify attributes of different quadrilaterals, such as rhombus, square, rectangle, parallelogram, and trapezoid; use the appropriate tools and technology to draw examples of make models of them.					*	X	X	X	X
Identify attributes of a circle, its radius, and its diameter; determine what distinguishes a circle from an oval shape.					*	X	X	X	X
Compare figures for congruency, similarity, or symmetry.					*	X	X	X	X
Demonstrate that angles of 90, 180, 270, and 360 Degrees relate respectively to $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$, and full rotations.					*	X	X	X	X
Verbalize, visualize, and make models for solid two-and three-dimensional geometric objects; describe shapes and solids in terms of vertices, edges, and faces.					*	X	X	X	X
Identify translations, reflections, and rotations around the center point of a polygon using concrete models.					*	X	X	X	X
Determine survey questions, collect data, and record this on a number line, graph, table and/or chart.					*	X	X	X	X
Identify the range, mode, and median for a set of data, and know what each statistic does and does not indicate about the data; use the statistics and data to make comparisons, draw a conclusion, or make a prediction of probability.					*	X	X	X	X
Locate the points corresponding to a numerical expression on graph paper and connect the points with a straight line; use this graph to determine the next probable point.					*	X	X	X	X
Describe the relationship between two sets of related data such as ordered pairs in a table or chart; specify locations and plot order pairs on a graph, map or globe.					*	X	X	X	X
Use Venn diagrams to sort and describe data.					*	X	X	X	X
Predict events according to the probability of likelihood of occurrence, using terms such as impossible, unlikely, equal, likely, and certain.					*	X	X	X	X
Convert numbers-as-figures to numbers-as-words and vice versa					*	X	X	X	X
Identify decimals, fractions, mixed numbers, and positive and negative integers on a number line; explore real-life situations where the use of these types of numbers is significant and necessary.					*	X	X	X	X
Use very large numbers, very small numbers, and decimals in addition, subtraction, multiplication, and division with and without a calculator.					*	X	X	X	X
Add, subtract, multiply, and divide with negative numbers.					*	X	X	X	X

Demonstrate proficiency with division, including long division with two digit divisors; explain the significance of a remainder in a real-life problem.						*	X	X	X
Recognize different interpretations of fractions as parts of a whole, parts of a set, and division of whole numbers by whole numbers.						*	X	X	X
Recognize percent as part-to-whole and part of a hundred; compute a given percent of a whole number; compare fractions, decimals, and percentages that are equivalent.						*	X	X	X
Investigate and justify why fractions need common denominators to be added or subtracted; explore the purpose of using equivalent forms in order to add and subtract fractions with unlike denominators.						*	X	X	X
Solve problems from real-life situations that involve fractions and mixed numbers in the operations of addition, subtraction, and multiplication, and express results in the simplest form; draw or construct models to verify conclusions						*	X	X	X
Identify and describe numbers according to their characteristics, including place value, prime or composite numbers, odd or even numbers and square numbers.						*	X	X	X
Identify and describe situations with constant or varying rates of change.						*	X	X	X
Recognize that change is often predictable when consistent patterns emerge; use algebraic expressions to describe the relationship in repeating, growing, and shrinking patterns.						*	X	X	X
Using a letter to represent an unknown number, write a simple algebraic expression with one variable, and evaluate by substitution.						*	X	X	X
Use commutative, associative, distributive, and inverse properties to simplify, perform, and check computations; apply these efficiently and accurately						*	X	X	X
Distinguish between situations when an estimate is appropriate and when an exact answer is needed.						*	X	X	X
Express problems and solutions using the proper and formal mathematical language and notation, supporting conclusions verbally and symbolically.						*	X	X	X
Use the appropriate tools, instruments, and technologies for taking various types of measurements.						*	X	X	X
Investigate formulas for the perimeter and area of a triangle and of a parallelogram, and compare these to the formulas for finding the perimeter and area of a rectangle.						*	X	X	X
Explain the differences among linear units, square units, and cubic units.						*	X	X	X

Identify and use the appropriate units of measure to find the perimeter, area, or volume of two- and three-dimensional objects; identify real-life situations where this knowledge is applicable.						*	X	X	X
Make conversions with measurement systems.						*	X	X	X
Compare temperatures in Celsius and Fahrenheit, recognizing the freezing and boiling point of water in each.						*	X	X	X
Add and subtract money in decimal notation.						*	X	X	X
Explore scale in drawings, models, and maps and relate scale to the measurement of real objects.						*	X	X	X
Solve problems involving elapsed time						*	X	X	X
Identify and draw angles, perpendicular and parallel lines, and various types of quadrilaterals and triangles using appropriate tools, such as ruler, compass, and protractor.						*	X	X	X
Determine relationships among the radius, diameter, center, and circumference of a circle.						*	X	X	X
Classify polygons as regular or irregular; continue to develop appropriate, formal vocabulary in all areas of geometry.						*	X	X	X
Solve problems by using the knowledge that the sum of the angles of any triangle is 180 degrees and the sum of the angles of a quadrilateral is 360 degrees.						*	X	X	X
Visualize and draw two-dimensional views of three-dimensional objects; construct a three-dimensional object from a two-dimensional representation.						*	X	X	X
Identify shapes that have reflectional symmetry and rotational symmetry.						*	X	X	X
Use concepts of position, direction, and orientation to describe objects in the classroom environment and beyond; explore what happens to the size, shape, and position of an object after sliding, flipping, turning, enlarging, or reducing it.						*	X	X	X
Answer questions about a real-life problem situation using information take from a graph						*	X	X	X
Use ordered pairs of numbers to locate and name points on a coordinate grid						*	X	X	X
Use tables of related number pairs to make line graphs						*	X	X	X
Know the measure of range, mean, median, and mode; and compare examples to show what each does and does not indicate and how they may differ.						*	X	X	X
Apply the use of fractions and percentages when comparing sets of data.						*	X	X	X
Determine whether or not a given graph matches a given set of data.						*	X	X	X

denominator to add two fractions or to find the reduced form of a fraction.									
Decompose and recompose whole numbers using factors and exponents; explain "squared" as being the same as the "second power" and "cubed" as the "third power"						*	X	X	
Write and analyze algebraic expressions using up to three variables and replacing the variables with given values.						*	X	X	
Use parentheses to group numbers and indicate which operation to perform first when writing expressions with more than two terms and different operations.						*	X	X	
Translate a problem, describe verbally or depicted in tables or graphs, into mathematical language; solve the problem mathematically, and then interpret that result in the original context.						*	X	X	
Identify relationships, distinguish relevant from irrelevant information, identify missing information, sequence and prioritize information, and observe patters as you solve problems.						*	X	X	
Express mathematical procedures and solutions clearly and logically, using the appropriate mathematical notation and language; use a variety of means such as words, numbers, symbols, charts, graphs, diagrams, and models to explain mathematical decisions and reasoning.						*	X	X	
Apply mathematics to solving everyday problems with other mathematical topics and with other curriculum subject areas.						*	X	X	
Use a problem-solving model that involves understanding the problem, making a plan, carrying out the plan, evaluating the solution for reasonableness, and explaining the procedures used and interpretation of results.						*	X	X	
Convert from one unit of measurement to another within customary U.S. system and within the metric system; use a formula to convert temperatures between Celsius and Fahrenheit.						*	X	X	
Solve problems involving rate, such as average speed, distance, and time; differentiate between rates and ratios.						*	X	X	
Know and use the formula for finding the circumference and area of a circle.						*	X	X	
Determine which measurement relates best to the context of a problem situation.						*	X	X	
Use variables in algebraic expressions to describe geometric formulas						*	X	X	
Identify measures of time, weight, and distance as fractions, mixed numbers and decimals; use this information to solve real-life mathematical situations.						*	X	X	

Describe, name, and draw vertical, adjacent, complementary, or supplementary angles.							*	X	X
Solve problems involving an unknown angle by using the properties of complementary and supplementary angles.							*	X	X
Use multiple classification criteria to describe triangles.							*	X	X
Identify and define relationships between lines.							*	X	X
Predict positions and orientations of two-dimensional shapes after transformations such as reflections, rotations, translations, and dilations; construct three-dimensional objects and sketch two-dimensional representations of each side; identify symmetry in three-dimensional shapes.							*	X	X
Draw two-dimensional shapes that are similar, though not congruent; use appropriate tools for measuring and constructing the shapes.							*	X	X
Compare the same data in different types of representations and determine which representation relates best to the context of the data.							*	X	X
Compute measures of central tendency and determine which provides the most useful information with regard to a specific question or given context.							*	X	X
Explain how additional data added to a set of data may affect the mean, median, and mode. Understand how the inclusion or exclusion of outliers affects measures of central tendency.							*	X	X
Compare samples of population with the data from the entire population; determine situations where it is reasonable to simply take a sample.							*	X	X
Identify ways of selecting a sample and what makes one sample more representative of the population.							*	X	X
Evaluate the validity of claims based on statistical data. Determine whether the manner in which a question is asked or the type of question it is may have influenced the results, or if the way the results were presented may have influenced the interpretation of results. Identify sampling errors and bias in the manner of presentation of results.							*	X	X
Represent data in an organized way, make logical inferences, and use the information to estimate the probability of future events or outcomes; understand that probability cannot determine an individual outcome, but can be used to predict the frequency of an outcome.							*	X	X
State probabilities as ratios, proportions, decimals between 0 and 1, and percentages between 0 and 100; know that if P is the probability of an event occurring, then 1-P is the probability of it not occurring.							*	X	X

